

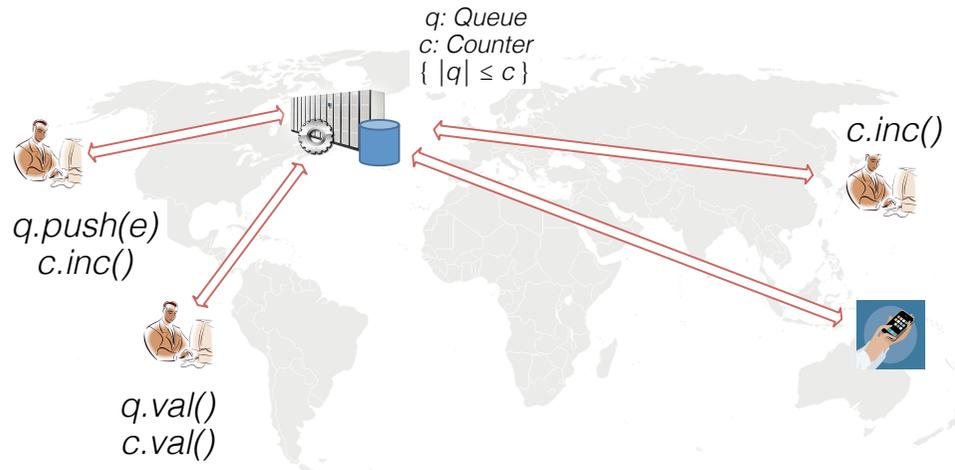
# Data consistency in 3D

*(It's the invariants, stupid)*

Marc Shapiro  
Masoud Saieda Ardekani  
Gustavo Petri



## Shared database



# This talk is about...

Understanding consistency

- Primitive consistency mechanisms
- How primitives compose models
- How models relate / differ
- What they cost

Understanding invariants

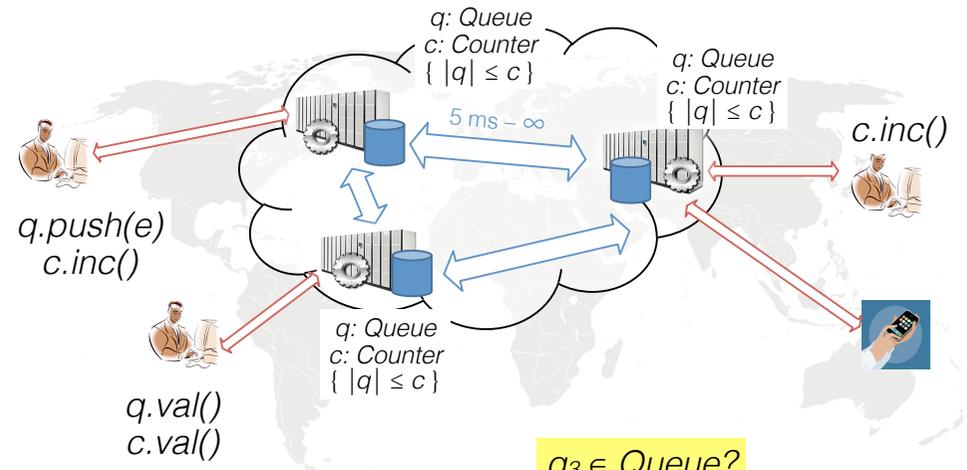
- Some interesting classes of invariants

Relating consistency to invariants

- Which primitives guarantee which invariants

Useful intuitions for app. and system designers

## Geo-replicated database



$q_3 \in \text{Queue?}$   
 $q_1 = q_2 ?$   
 $|q_1| \leq c_4 ?$

# Consistency

More replicas:

- Better read availability, responsiveness, performance, etc.
- More work to keep replicas in sync

Consistent = behavior similar to sequential:

- Satisfies specs: does  $q$  behave like a queue?
- Replicas agree: is  $q$  identical everywhere?
- Objects agree: is  $|q| \leq c$ ?
- Same flow of time?  $q1.push()$  before  $q2.push()$

[Consistency in 3D]

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# Consistency opportunities and costs

CAP

Availability

- ⇒ Parallelism keeps the hardware busy
- ⇒ More implem. options, scalable

But consistency constrains order of events:

- Delay delivery
- Stale reads
- Waits, synchronisation (mutual wait)

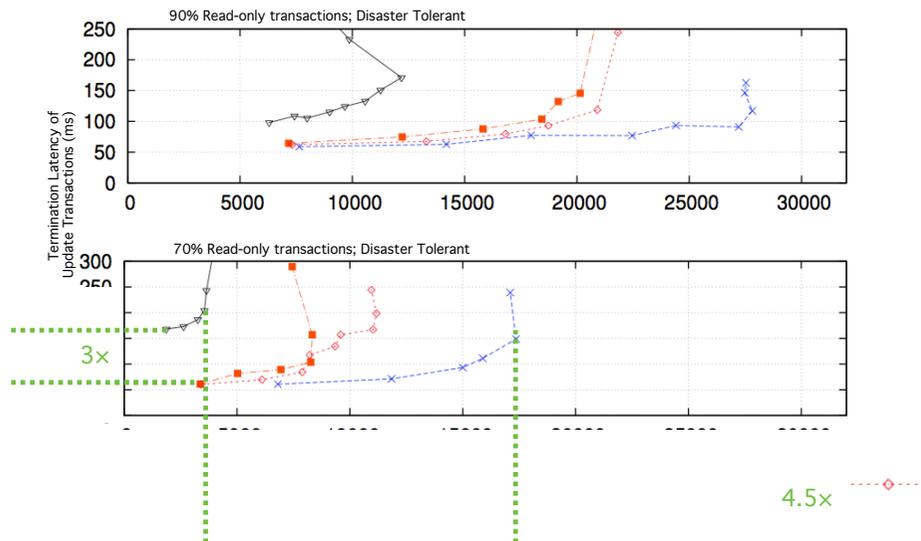
Keeping track of order requires metadata

Significant!

[Consistency in 3D]

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## Costs illustrated

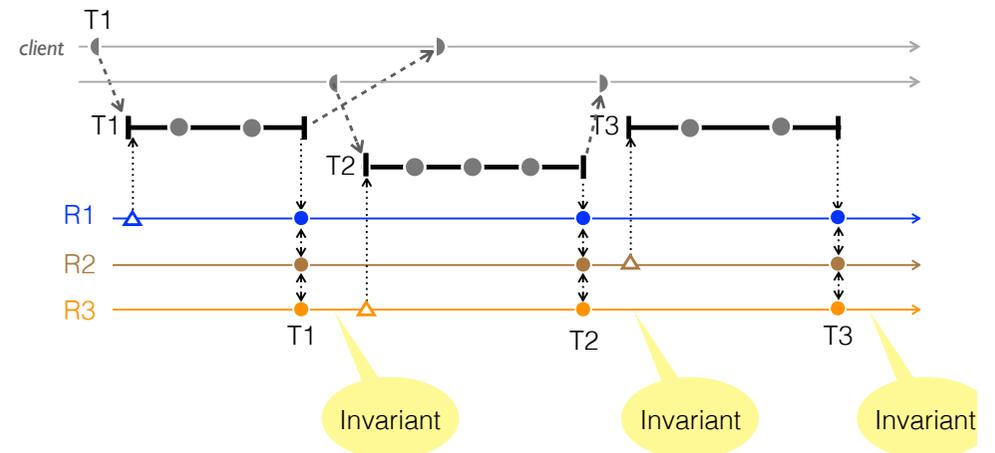


[Consistency in 3D]

Credit: Masoud Saeida Ardekani

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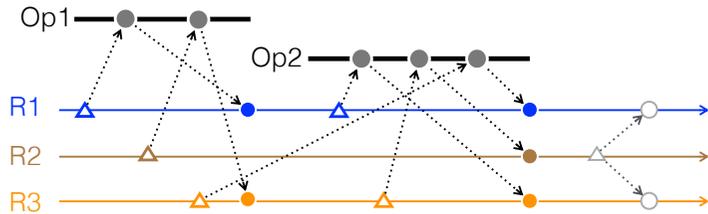
## Strict Serialisability



[Consistency in 3D]

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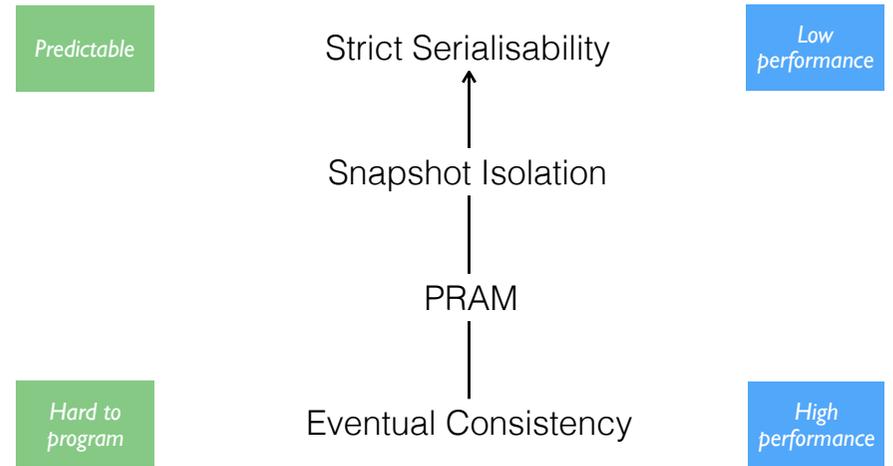
# Eventual consistency



[Consistency in 3D]

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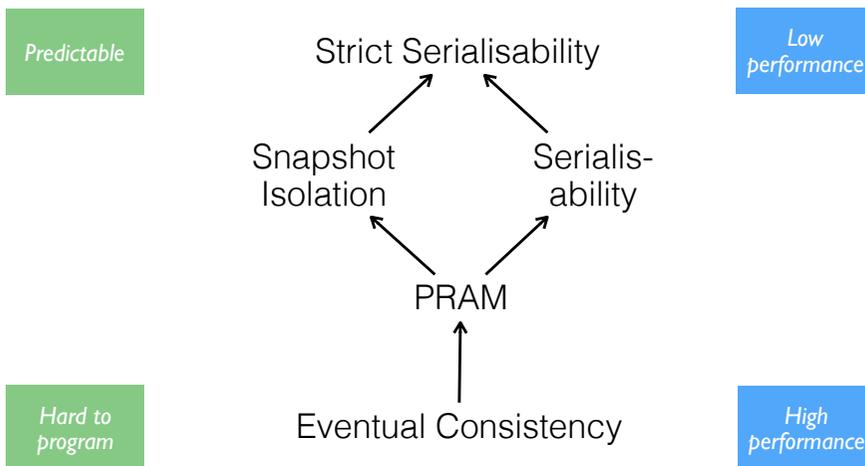
# Strong vs. weak?



[Consistency in 3D]

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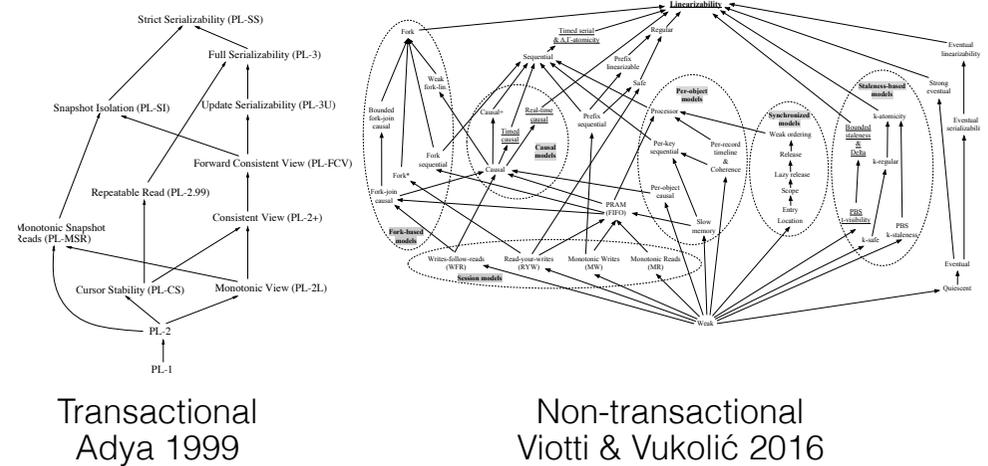
# Strong vs. weak?



[Consistency in 3D]

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# Strong vs. weak?



[Consistency in 3D]

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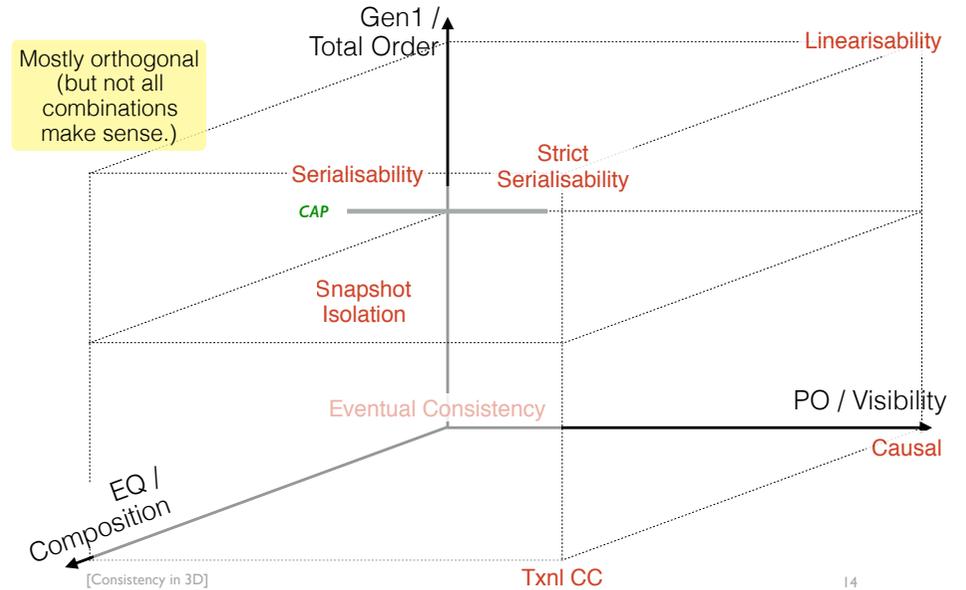
# Three classes...

	...of invariant	... of protocol
Gen1	Object value	Total order of operations
PO	Relative ordering of operations	Visibility
EQ	State equivalence	Composition

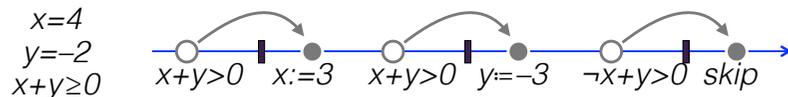
[Consistency in 3D]

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# Three dimensions



# Operation



*generator*: read, compute, generate effector

*effector*: compute, write side-effect

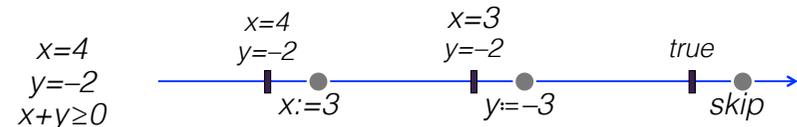
Sequential execution:

- precondition  $\Rightarrow$  invariant
- each effector individually safe

[Consistency in 3D]

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# Sequential correctness



*generator*: read, compute, generate effector

*effector*: compute, write side-effect

Sequential execution:

- precondition  $\Rightarrow$  invariant
- each effector individually safe

[Consistency in 3D]

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# Guarantee vs. semantics

Guarantee:

- Class of invariants that is always true
- Regardless of application code
- Assuming sequentially correct

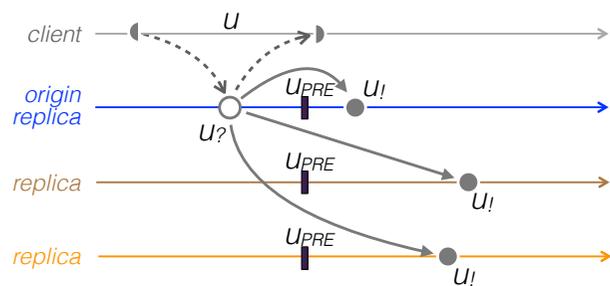
Application can compensate for absence of guarantee

- e.g.  $Inv = \{ c \geq 0 \}$ , app:  $c.inc()$

[Consistency in 3D]

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## Replicated operation



$u: state \rightsquigarrow (retval, (state \rightsquigarrow state))$

Read one, write all (ROWA)

Deferred-update replication (DUR)

[Consistency in 3D]

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# Data types

Register

- Update: assign with constant
  - Not commutative
  - Absorbing

High-level types

- Counter, ORset, Sequence: effectors commute
- Stock, Account, Queue:  $\neg$  commute

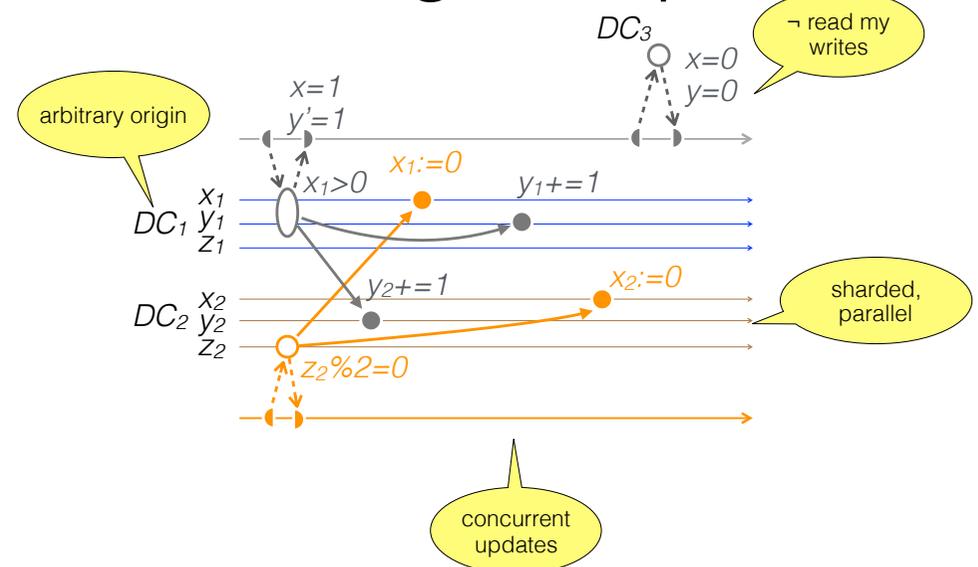
Composed data

- + structural invariants

[Consistency in 3D]

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## Sharded, geo-replicated

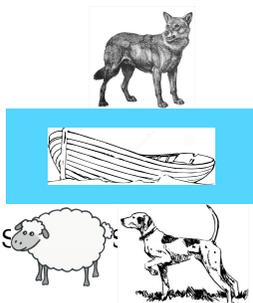


[Consistency in 3D]

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# Type EQ invariants

- $A = B$
- $x.friendOf(y) \Leftrightarrow y.friendOf(x)$
- $x + y = constant$
- $South \sqcup Boat \sqcup North$   
= { sheep, dog, wolf }



Joint update to two objects

Atomicity (all-or-nothing) property of trans

Protocol: single update message

- Asynchronous

# EQ: transactional composition

Airplane reservation

- Allocate a seat to me
- Pay for the flight

Two EQ relations:

- paid = have\_seat
- my \$\$ + airline \$\$ = constant

Ad-hoc grouping

(This txn also needs TO + snapshot)

# EQ/Composition axis

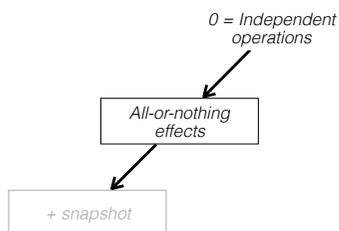
Transaction groups operations

All-or-nothing effects:

- Deliver effectors indivisibly
  - packaged together
- + same TOE
- ≈ 2-phase commit

Snapshot reads:

- all generators read from same set of effectors
  - maintain versions
- + same TO, VIS guarantees
  - coordination



# EQ/Composition axis

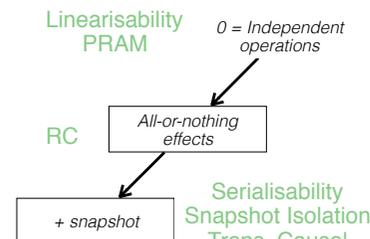
Transaction groups operations

All-or-nothing effects:

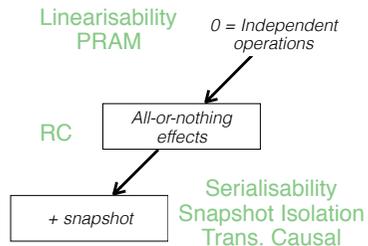
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# EQ/Composition axis



Transaction groups operations

All-or-nothing effects:

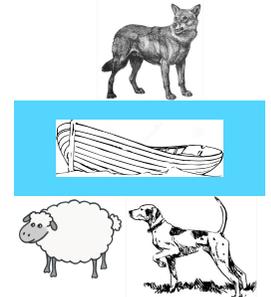
- Deliver effectors indivisibly
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Snapshot reads:

- all generators read from same set of effectors
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  - coordination

# Type PO invariants

- $employee.manager.salary \geq employee.salary$
- $S1; S2; S3 \equiv S1 \Leftarrow S2 \Leftarrow S3$
- $dog \in S \Leftarrow sheep \in S \wedge wolf \in S$
- Referential integrity  
"inode references disk block"
- $ACL(u, p) \Leftarrow access(u, p)$



Demarcation Protocol:

1. increase LHS by  $c$
  2. increase RHS by  $c' \leq c$
- $\Rightarrow$  ordered delivery

No synchronisation: Available

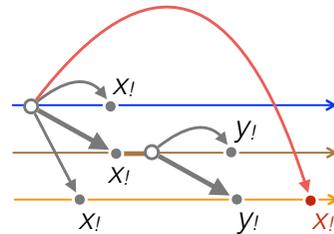
# PO: transitive / causal visibility

$x = 100; y = 100$

$Inv = \{ x \geq y \}$

Ex 1:

- P1:  $x += 100$
- P2: if  $x > y$  then  $y += (x-y)/2$
- P3:  $x \geq y$ ?
- Transitive visibility  $vis^* \subseteq vis$



# PO: transitive / causal visibility

$x = 100; y = 100$

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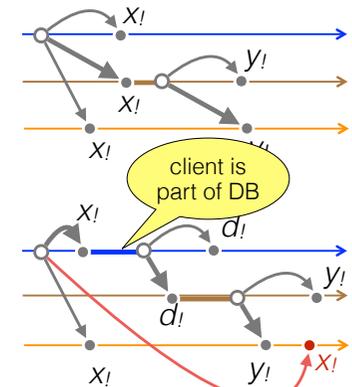
Ex 1:

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- P3:  $x \geq y$ ?
- Transitive visibility  $vis^* \subseteq vis$

Ex 2:

- P1:  $x += 100; d := 100$
- P2: if  $d > 0$  then  $y += d/2$
- P3:  $x \geq y$ ?

Causal visibility  $(vis; po)^* \subseteq vis$



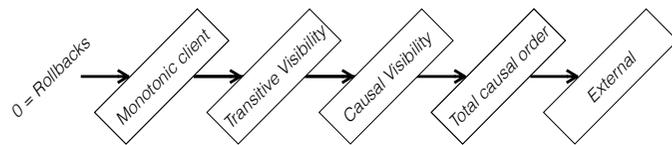
# PO/Visibility axis

## Visibility

- Which *writes* visible to *reads* Sender not delayed  $\Rightarrow$  writes available

## Transitive closure property

- Metadata
  - System-wide
- Stale data  $\Rightarrow$  reads available



[Consistency in 3D]

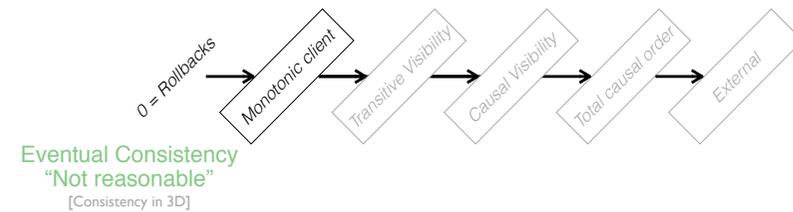
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# Monotonic client

- Read My Writes
- Monotonic Reads

Often assumed

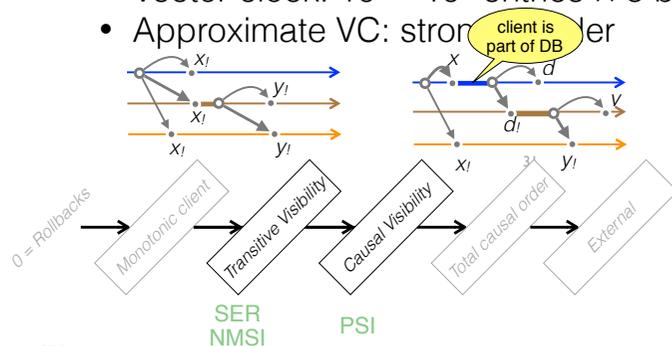
- Buffer



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# Transitive, causal vis.

- Effector: metadata identifies set of predecessor effectors
- Delay delivery after predecessors
  - Read stale data
- Graph: unbounded
- Vector clock:  $10^4$ — $10^6$  entries  $\times$  8 bytes!
- Approximate VC: strong  $\Rightarrow$  client is part of DB



[Consistency in 3D]

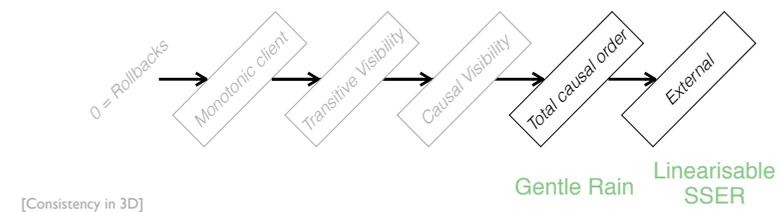
# Total/external causal

Total order extends causal order

Metadata: 1 single scalar

- but cost of total order

External: real-time clock



[Consistency in 3D]

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# Gen1 invariants

$Inv = "0 \leq x"$   
 $u_i = "x := x-1"$   
 $\{ Inv \wedge 1 \leq x \} u_i \{ Inv \}$

Predict that  $Inv$  will be true after  $u_i$ :

- Sequential: weakest precondition
- Generalises to bounded concurrency

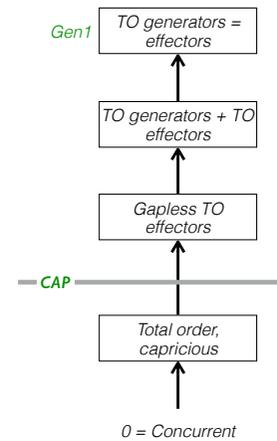
Unbounded concurrency: no sufficient precondition

- Invariant is not stable
- Limit concurrency: escrow
- No concurrency: order updates

# Gen1: total order

Do replicas observe events in the same order?

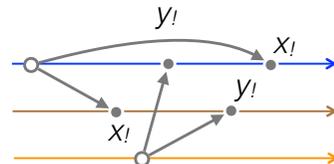
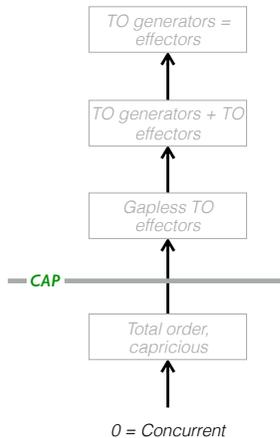
Pick a unique number



# 0 = unordered

Do replicas observe events in the same order?

Pick a unique number



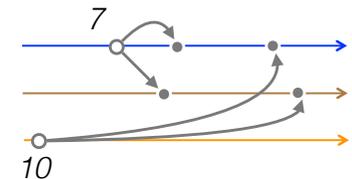
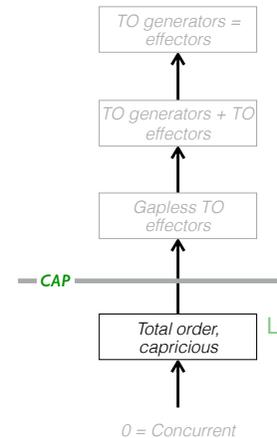
No: concurrent

- Commute  $\Rightarrow$  converge
- Stable precondition  $\Rightarrow$  Invariant

# Capricious TO effectors

Do replicas observe events in the same order?

Pick a unique number

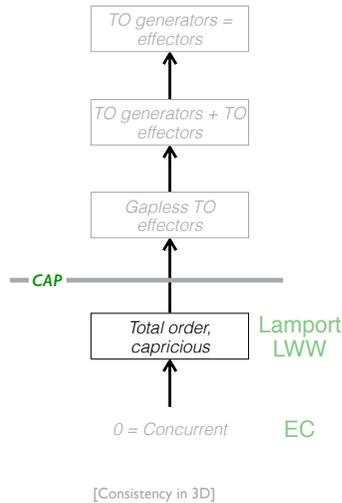


Pick a number locally: capricious

Gap: will arrive later?

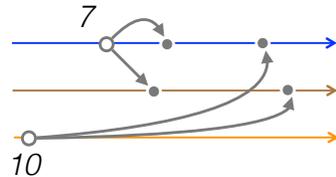
- Non-monotonic: rollback
- Monotonic
  - Wait for gap to fill (Lamport 78)
  - Lost updates (LWW)

# Capricious TO effectors



Do replicas observe events in the same order?

Pick a unique number



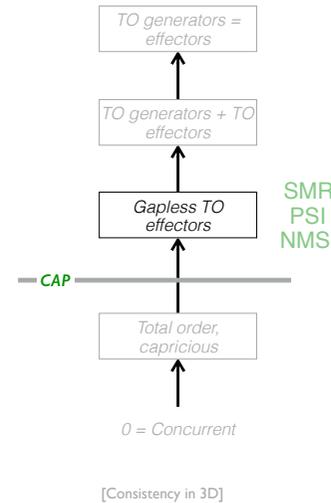
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[Consistency in 3D]

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# Gapless TO effectors

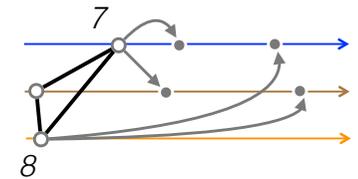


Do replicas observe events in the same order?

Pick a unique number

Gapless:

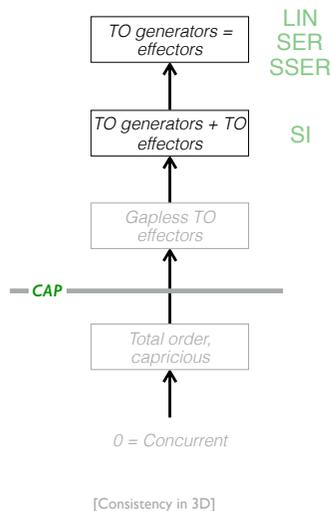
- No lost updates
  - Consensus, 2PC to uniquely allocate next free number
- ⇒ not available



[Consistency in 3D]

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# TO generators



Do replicas observe events in the same order?

Pick a unique number

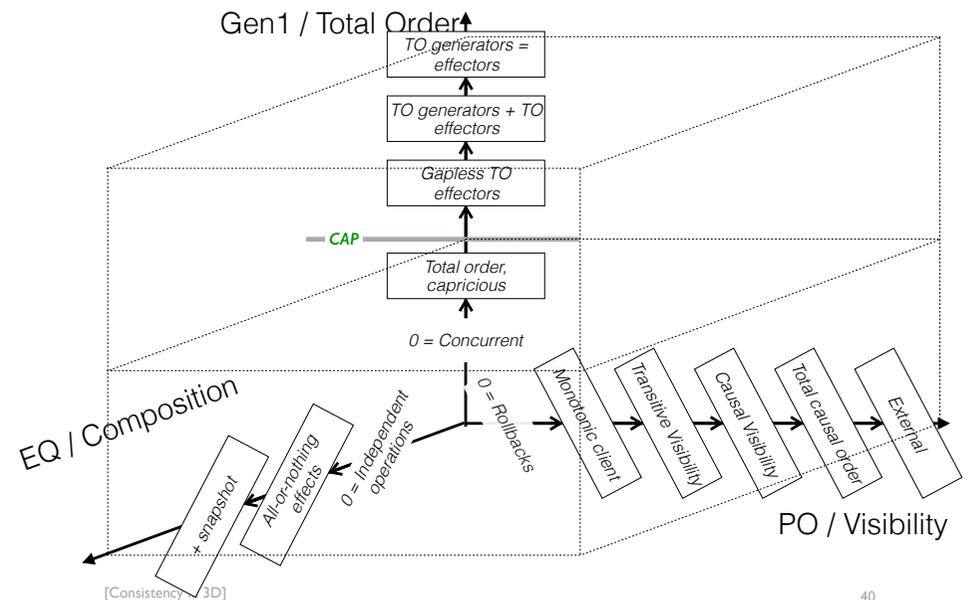
TO effectors

- + TO generators
  - separate from effectors
  - same order as effectors

[Consistency in 3D]

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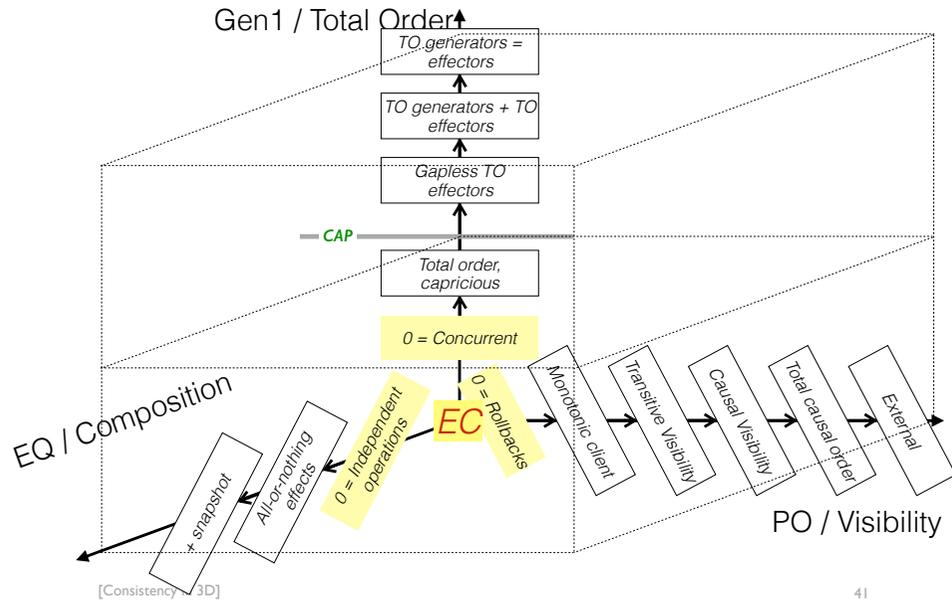
# Three dimensions



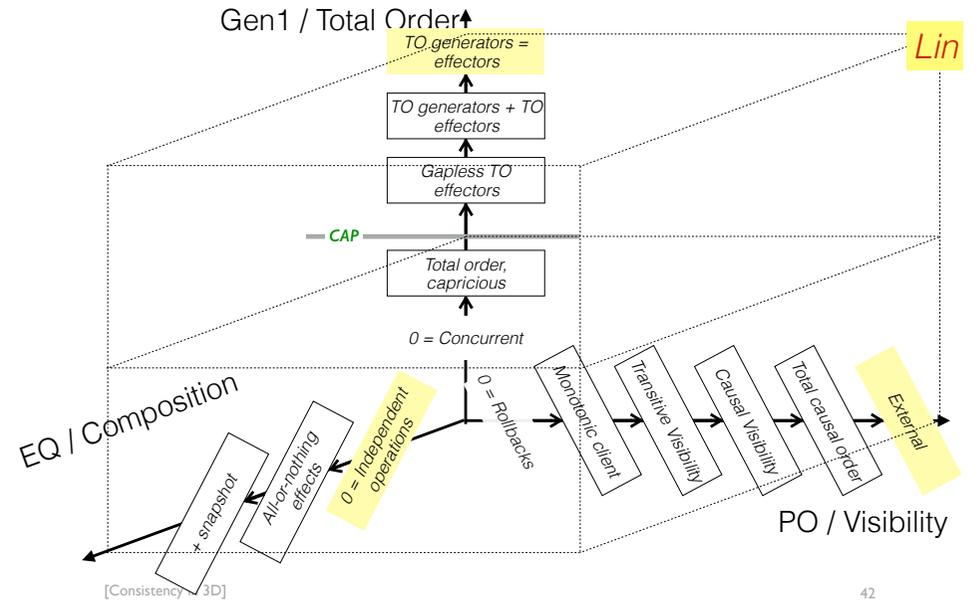
[Consistency in 3D]

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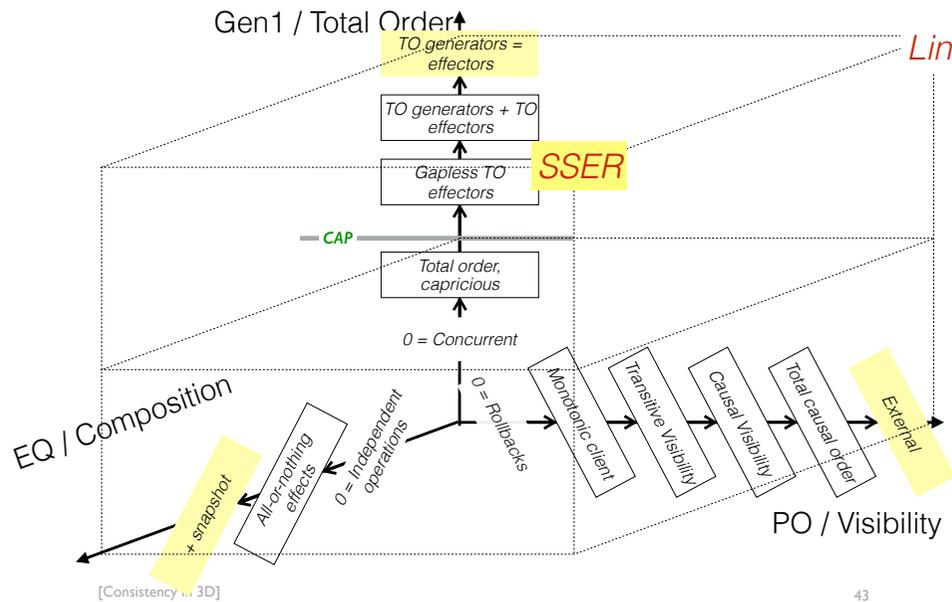
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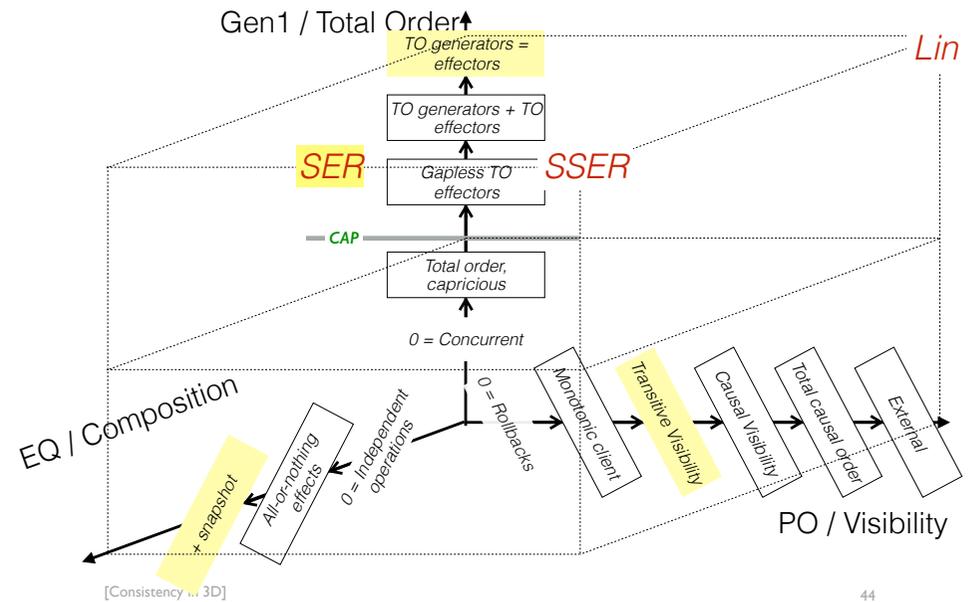
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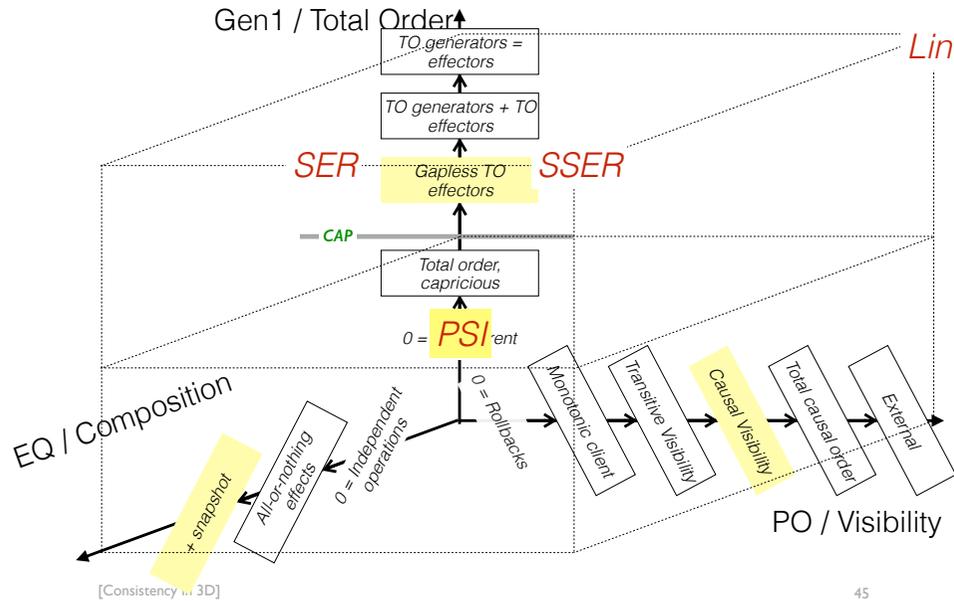
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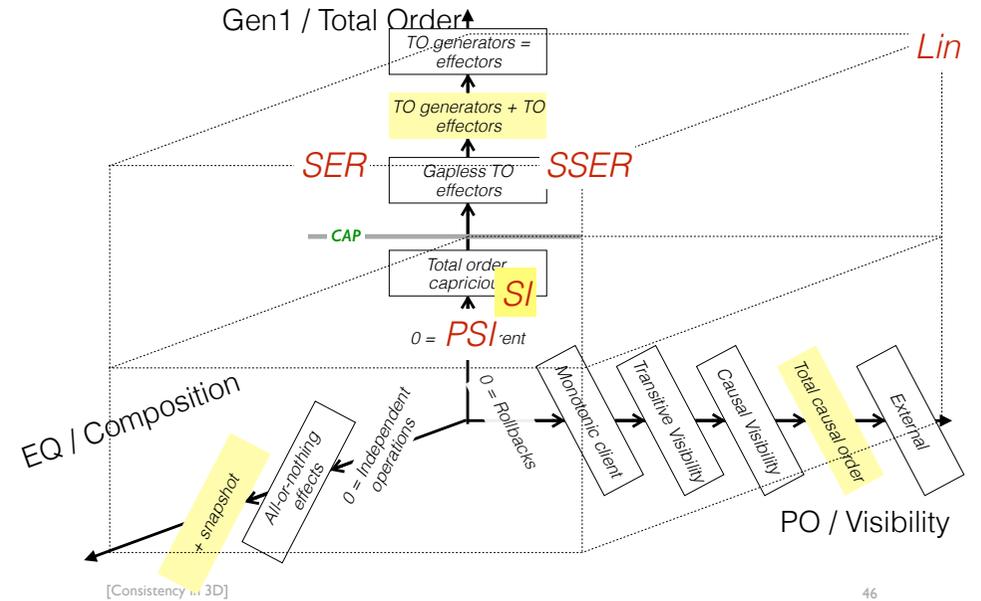
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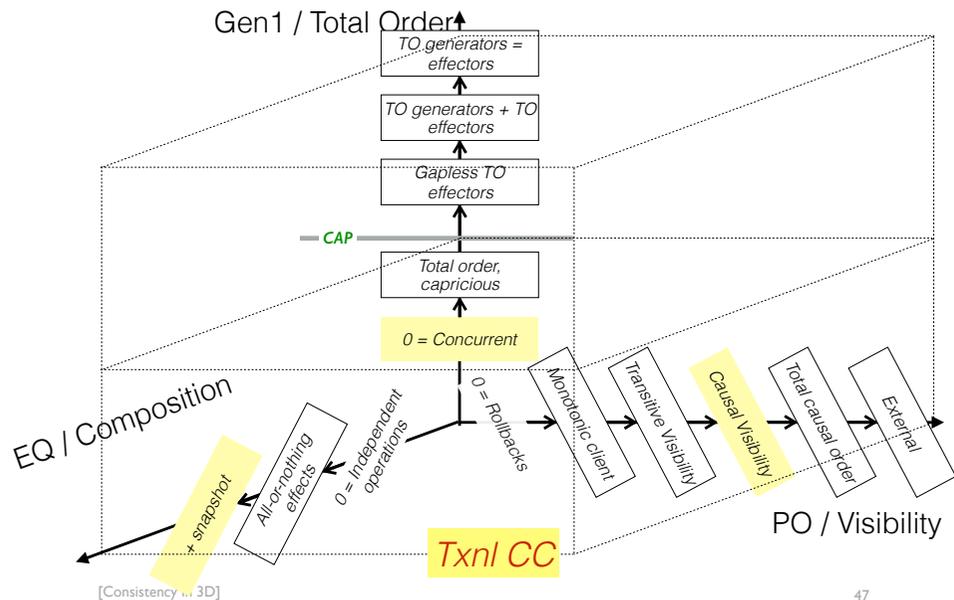
# Three dimensions



# Three dimensions



# Three dimensions



Total Order	Composition	Visibility				
		Rollbacks	Monotonic	Transitive	Causal	External
TOG=TOE	All-or-Nothing + Snapshot			SER		SSER
	All-or-Nothing Effectors Single Operation					
Gapless TOE	All-or-Nothing + Snapshot			NMSI	PSI	SSI
	All-or-Nothing Effectors Single Operation					
Capricious TOE	All-or-Nothing + Snapshot	Bayou				∅
	All-or-Nothing Effectors Single Operation		LWW			∅
Concurrent Ops	All-or-Nothing + Snapshot				Causal HAT	∅
	All-or-Nothing Effectors Single Operation	EC	RC PRAM		CC	∅

# Summary

Distributed, replicated data

- Improves read availability
- Parallel updates may violate invariants
- Guarantee: invariants maintained by system
- System vs. application cost trade-off
  - Tools needed

3D consistency design space

- Total order (effectors, generators)
- Visibility order
- Transactional Composition

Work in progress

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## 4 session guarantees ≡ causal

